

Propriedades das Transformadas de Laplace

$\mathcal{L}[A f(t)] = A F(s)$
$\mathcal{L}[f_1(t) \pm f_2(t)] = F_1(s) \pm F_2(s)$
$\mathcal{L}\left[\frac{d}{dt} f(t)\right] = sF(s) - f(0\pm)$
$\mathcal{L}\left[\frac{d^2}{dt^2} f(t)\right] = s^2 F(s) - sf(0\pm) - f'(0\pm)$
$\mathcal{L}\left[\frac{d^n}{dt^n} f(t)\right] = s^n F(s) - \sum_{k=1}^n s^{n-k} f(0\pm) \quad \text{onde } f(t)^{(k-1)} = \left[\frac{d^{k-1}}{dt^{k-1}} f(t)\right]$
$\mathcal{L}\left[\int f(t) dt\right] = \frac{F(s)}{s} + \frac{1}{s} \left[\int f(t) dt\right]_{t=0\pm}$
$\mathcal{L}\left[\int \dots \int f(t) (dt)^n\right] = \frac{F(s)}{s^n} + \sum_{k=1}^n \frac{1}{s^{n-k+1}} \left[\int \dots \int f(t) (dt)^k\right]_{t=0\pm}$
$\mathcal{L}\left[\int_0^t f(t) dt\right] = \frac{F(s)}{s}$
$\int_0^\infty f(t) dt = \lim_{s \rightarrow 0} F(s) \quad \text{se } \int_0^\infty f(t) dt \text{ existir}$
$\mathcal{L}[e^{-at} f(t)] = F(s+a)$
$\mathcal{L}[f(t-a)1(t-a)] = e^{-as} F(s) \quad a \geq 0$
$\mathcal{L}[tf(t)] = -\frac{dF(s)}{ds}$
$\mathcal{L}[t^2 f(t)] = \frac{d^2 F(s)}{ds^2}$
$\mathcal{L}[t^n f(t)] = (-1)^n \frac{d^n F(s)}{ds^n} \quad n=1,2,3..$
$\mathcal{L}\left[\frac{1}{t} f(t)\right] = \int_s^\infty F(s) ds \quad \text{se } \lim_{t \rightarrow 0} \frac{1}{t} f(t) \text{ existir}$
$\mathcal{L}\left[f\left(\frac{t}{a}\right)\right] = aF(as)$
$\mathcal{L}\left[\int_0^t f_1(t-\tau) f_2(\tau) d\tau\right] = F_1(s) F_2(s)$
$\mathcal{L}[f(t)g(t)] = \frac{1}{2\pi j} \int_{c-j\infty}^{c+j\infty} F(p)G(s-p) dp$